## Worksheet 1.2 - Math 455

1. Show that if $A$ is the adjacency matrix of some graph $G$, then $\left[A^{k}\right]_{i, j}=0$ for all $1 \leq k<d\left(v_{i}, v_{j}\right)$.
2. Find $A^{3}$ where $A$ is the adjacency matrix of $K_{4}$ without computing it directly.
3. If $A$ is the adjacency matrix of some graph $G$, show that $\left[A^{2}\right]_{j, j}=\operatorname{deg}\left(v_{j}\right)$.
