Math 128	Exam #2	Fall 2017	SPECIAL CODE: 111401				
Name	Solns	— F	20	Exam	2		
Signature:				Versia			

Academic Honesty Statement: By signing my name above, I acknowledge that I understand each of the following behaviors:

using a calculator or cell phone (or any other communication technology); referring to a piece of paper or object with helpful information on it (cheat sheet, notes, etc...); looking at a test or answer sheet that is not my own; allowing another student to look at my test or answer sheet; communicating with other students (verbally or nonverbally); taking the test for another student; taking my bubble sheet of answers with me when I've finished; talking while waiting to hand in my test materials to the proctors; sharing a calculator

to be a form of academic dishonesty (cheating). I am also pledging not to engage in any of these behaviors. I understand that if I do engage in these behaviors, the consequences will be failure of the exam and a formal charge of academic dishonesty to the Ombuds Office.

Please shut off all cell phones, ear phones, computers, beepers, smart watches, etc...

Please put everything away except a #2 pencil and a calculator that is NOT your cell phone. You may write on the test. There are twenty five multiple choice questions and each question is worth four points.

1. On the bubble sheet, where it says "Name," please print your last name, leave a space, and then print your first name in the rectangles. Then fill in the bubbles underneath.

2. On the bubble sheet, where it says "Identification Number," please write your entire Student ID number in the rectangles and fill in the bubbles underneath. Please double check to make sure you bubbled in your ID # correctly.

4. On the bubble sheet, where it says "Special Codes," please write the numbers: 111401 in the rectangles and fill in the bubbles underneath. Please double check to make sure you bubbled in the special code correctly.

Please make sure you bubble in your answers carefully on the bubble sheet and **circle your answers on your test booklet**.

Formulas:

Partial Derivatives:

$$f_x(x, y) = \lim_{h \to 0} \frac{f(x + h, y) - f(x, y)}{h}$$
$$f_y(x, y) = \lim_{h \to 0} \frac{f(x, y + h) - f(x, y)}{h}$$

Linear Approximation:

$$f(x, y) \approx f(a, b) + f_x(a, b)\Delta x + f_y(a, b)\Delta y$$

Normally Distributed Density Function:

$$p(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

Uniformly Distributed Density Function:

$$p(x) = \frac{1}{b-a}$$

Exponentially Distributed Density Function:

$$p(t) = ke^{-kt}$$

Mean:

$$\mu = \int_{-\infty}^{\infty} x p(x) dx$$

Median:

$$\int_{-\infty}^{T} p(x) dx = 0.5$$

1.) Given  $p(x) = kx^2$  where  $0 \le x \le 2$ , find the value of k that will make this function a PDF.



2.) Suppose P(t) is a CDF with PDF p(t) on  $a \le t \le b$ . Which of the following is always true?



3.) The PDF of the GPA of students at a university is shown below.



Approximately what fraction of the students had a GPA of 2 or greater?



4.) The distribution of IQs can be modeled by a Normal Distribution with mean 100 and standard deviation 15. Approximately what fraction of the population has an IQ between 85 and 115?



5.) The table below shows the value of a CDF, P(x), of household income distribution in the United States in 2006. What percentage of households made between \$60,000 and \$100,000?

Income $x$ (thousand \$)	20	40	60	80	100	150	
P(x) (%)	21.7	45.4	63.0	75.8	84.0	94.0	
(A) 84%		P()	( = 6	60K	) =	63	2/0
(B) 63%		P(x)	5 100	oK)	= °	799°1	0
(C) 21%							
(D) There is not enough inf	ormation	1.		$\sim$		$(\pi)$	(3) /
⇒ P(	GO K	人上	X £	100 /	= = [	21	0/0

6.) For what value of *a* does the graph represent a PDF?



or calculator 7.) The annual rainfall in Massachusetts is a random variable with probability density function defined by  $\frac{1}{150}(2x+5)$  on  $0 \le x \le 10$ . Find the mean annual rainfall. っ

(A) 5.0  
(B) 3.194  
(C) 1.0  
(D) 5.111  

$$= \frac{1}{150} \int_{0}^{10} 2\chi^{2} + 5\chi d\chi = \frac{1}{150} \left[\frac{3}{2}\chi^{3} + \frac{5}{2}\chi^{8} \right]_{0}^{10} = \frac{1}{150} \left[\frac{3}{2}\chi^{2} + 5\chi d\chi = \frac{1}{150} \left[\frac{3}{2}\chi^{3} + \frac{5}{2}\chi^{8} \right]_{0}^{10} = \frac{1}{150} \left[\frac{2000}{3} + \frac{5}{2}\right]_{0}^{2} - (0+0) = \frac{1}{150} \left[\frac{2000}{3} + 250\right] = \frac{1}{3} \frac{2759}{159} = \frac{1}{3} \frac{2759}{3} = \frac{55}{3} = \frac{55}{9} = 6.1111...$$

8.) Wait times at a traffic light are exponentially distributed with probability density function  $p(t) = 0.07e^{-0.07t}$ , where t is measured in minutes  $0 \le t < \infty$ . Find the median wait time at the traffic light.

 $P(t) = K \bar{e}^{Kt}$  (sometimes we) use  $\lambda$  instead of K) 9.9 minutes (B) 7 minutes > K = 0,07 (C) 47.9 minutes  $\frac{\mathcal{E}_{\text{Kponential Distribution}}}{\mathcal{M}_{\text{Eqn}}} = \frac{1}{K} = \frac{1}{K}$ (D) 35 minutes  $L \implies T = \frac{100}{0.07}$  $L \implies T = \frac{100}{0.07}$  $L \implies T = \frac{100}{0.07}$ medius - lu 2

9.) Given that X is a random variable on  $12 \le x \le 20$  with a CDF of



10.) The clotting time of blood is normally distributed with mean of 7.35 seconds and standard deviation of 0.35 seconds. What is the probability that the blood clotting time will be less than 7 seconds?

- 0.1429 (A)
- **(B)** 0.8414
- (C)0.3362
- 0.1587 (D)

 $\mu = 7.35 \quad 6 = 0.35$   $P(x \leftarrow 7) = \int_{-x^{2}}^{7} \int_{0.35}^{1} \int_{2\pi}^{7} e^{-\frac{(x-7.35)^{2}}{2(0.35)^{2}}} dx$   $e^{-x^{2}} = \int_{0}^{7} \int_{-x^{2}}^{1} e^{-\frac{(x-7.35)^{2}}{2(0.35)^{2}}} dx$   $e^{-x^{2}} = \int_{0}^{7} \int_{-x^{2}}^{1} e^{-\frac{(x-7.35)^{2}}{2(0.35)^{2}}} dx$   $e^{-x^{2}} = \int_{0}^{7} \int_{0}^{1} \int_{-x^{2}}^{1} e^{-\frac{(x-7.35)^{2}}{2(0.35)^{2}}} dx$ 



12.) Wait times are the bank are exponentially distributed with PDF of  $p(t) = 0.04e^{-0.04t}$  on  $0 \le t < \infty$ . Find the CDF.



13.) Suppose that p(x) is a probability density function and P(x) is a cumulative distribution function for the same distribution. Which of the following represents the fraction of the population between x = 3 and x = 6?



14.) The temperature adjusted for wind-chill is a temperature which tells you how cold it feels, as a result of the combination of wind and temperature. If the temperature is 10°F and the wind speed is 20 mph, here cold does it feel?

