

1.[12 points] [Calculators are not allowed on this question] Let $f(x) = xe^x$ and let $F(x) = xe^x - e^x + \pi$. Show by differentiating $F(x)$ that F is an anti-derivative of f . Show all your work.

2.[16 points] Let $F(x) = \int_1^{\cos x} e^{\sin t} dt$

(a) Find $F'(x)$

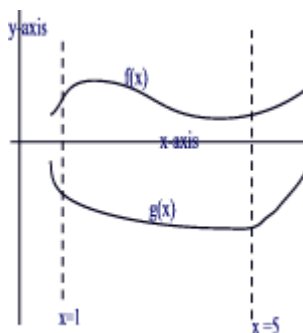
(b) Find $F(2\pi)$

3.[12 points] If $\int_1^7 f(x)dx = 19$ and $\int_1^5 f(x)dx = 25$ find:

(a) $\int_5^7 f(x)dx$

(b) $\int_1^5 3f(x)dx$

4.[12 points] If $0 \leq f(x)$ and $g(x) \leq 0$ for $1 \leq x \leq 5$, $\int_1^5 f(x)dx = 10$, and $\int_1^5 g(x)dx = -30$. The graph looks like:



Find

(a) The area of the region bounded by $x = 1$, $x = 5$, $y = f(x)$, and $y = g(x)$

(b) $\int_1^5 |g(x) - f(x)| dx$

(c) $\int_1^5 (g(x) + f(x)) dx$

5.[10 points] Use the substitution rule to show that

$$\int_0^{10} x^2 e^{x^3} dx = \frac{1}{3} \int_0^{1000} e^u du$$

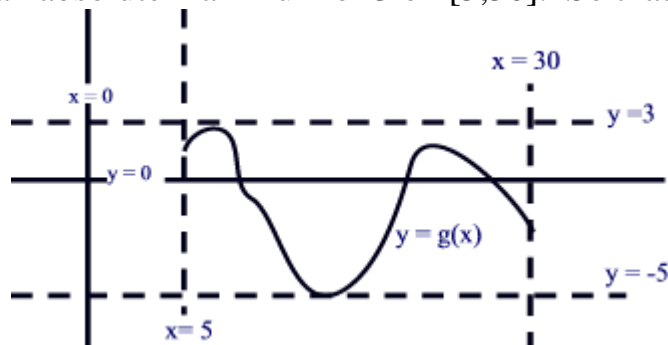
6.[10 points] Let R be the region of the plane bounded by $y = x^2 + 2$ and $y = x^3 + 2$. Find the area of R .

7.[10 points] Let R be the region of the plane bounded by $y^2 - 2 = x$ and $y = x$. Find the area of R.

8.[20 points] From the top of a 192 feet tall building a ball is thrown up with an initial velocity of 64 ft/sec. The acceleration due to gravity is -32 ft/sec^2 . Assuming that the only force acting on the ball is gravity find:

- The velocity function.
- The position function.
- The time the ball takes to reach the ground.
- The total distance traveled by the ball.
- The displacement of the ball.

[10 points] Let $g(x)$ be a continuous function on $[5, 30]$ and with g having an absolute minimum of -5 and an absolute maximum of 3 on $[5, 30]$. So that the graph looks like:



Show that:

$$(a) -125 \leq \int_5^{30} g(x) dx \leq 75$$

$$(b) 0 \leq \int_5^{30} |g(x)| dx \leq 125$$