For full credit you must present a clearly organized solution, showing all supporting calculations. Include appropriate units in your final answers.

1. An open top box with a square base is to be made by cutting four squares away from the corners of a $4\,\text{ft} \times 4\,\text{ft}$ square piece of cardboard, and then folding up the sides. Find the maximum volume possible and the dimensions of the box achieving it.