Math 612 Homework 3

Due February 25 to Gradescope (by 11:59 pm)

The problem numbers below refer to Dummit and Foote, third edition.

Homework policies:

- 1. Homeworks will vary in length from 10 20 problems, depending on length and difficulty of the problems. A subset of the problems will be graded for correctness.
- 2. You can neatly handwrite or type your homework, and do not need to copy the problem statement. Please clearly label each problem with its number/part.
- 3. You may use any result from a previous section of the textbook or previous homework assignment. Please indicate that you have done so (e.g. 'by Proposition 2 in §1.1, part (2) ... ' or 'by Homework 2, Problem 4...').
- 4. If you collaborate with others, please write their names at the top of your assignment.
- 5. For most homework assignments, I will include 1 2 sample qualifying exam problems related to the content of the assignment. You *do not* have to complete these problems or turn them in, but they are good indications of your mastery of the material.

Assigned problems:

- §13.5: 3, 4, 5, 10
- §13.6: 3, 5, 8

Sample qualifying problem related to this section:

Spring 2019 Exam, Problem 8: Let K be a finite field and let L be an extension of K of degree n. Fix a monic irreducible polynomial $f \in K[x]$ of degree d dividing n. Show that there is $\alpha \in L$ which has minimal polynomial f over K.