## Math 611 Homework 2

Due September 22, 2023 to Gradescope (by 11:59 pm)

The problem numbers below refer to Dummit and Foote, third edition.

## Homework policies:

- 1. Homeworks will vary in length from 10 20 problems, depending on length and difficulty of the problems. A subset of the problems will be graded for correctness.
- 2. You can neatly handwrite or type your homework, and do not need to copy the problem statement. Please clearly label each problem with its number/part.
- 3. You may use any result from a previous section of the textbook or previous homework assignment. Please indicate that you have done so (e.g. 'by Proposition 2 in §1.1, part (2) ... ' or 'by Homework 2, Problem 4...').
- 4. If you collaborate with others, please write their names at the top of your assignment.
- 5. For most homework assignments, I will include 1 2 sample qualifying exam problems related to the content of the assignment. You *do not* have to complete these problems or turn them in, but they are good indications of your mastery of the material.

## Assigned problems:

- §1.6: 6, 9, 13, 14, 18
- §1.7: 4, 18, 19, 21
- §2.1: 2, 6, 9, 12
- §2.2: 4, 6, 7, 10

Sample qualifying problem related to this section:

Fall 2017 Exam, Problem 3: let G be a group acting faithfully on a set X of five elements. Suppose this action has exactly two orbits, one of size 2 and the other of size 3. Up to isomorphism, what possible groups could G be?

Fall 2022 Exam, Problem 2(b): let p be a prime and let H be the subset of upper triangular matrices in  $GL_2(\mathbb{F}_p)$  with 1's on the diagonal. Prove that the center of H is

$$Z(H) = \left\{ \begin{bmatrix} 1 & 0 & c \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \mid c \in \mathbb{F}_p \right\}.$$